

# Introduction to Cryptography

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m0leCon 2025 Workshops

# What is cryptography?

- Where is cryptography?
  - What is cryptography about?
  - Kerchoff's principle
  - Classification of encryption / decryption algorithms
  - An easy example of encryption: Caesar cipher
-

# Where is Cryptography?

Nowadays cryptography is found **anywhere**

- Internet communications (SSL, HTTPS...)
- Mobile networks (e.g. GSM)
- Messaging applications (e.g. Signal, WhatsApp)
- Legal documentations (digital signatures)
- Credit-card transactions over Internet
- Blockchains
- ... many more!

# What is Cryptography about?

- Hiding data
  - Encryption: takes a secret key and the data to hide (plaintext) and returns a bunch of random looking bytes (ciphertext)
  - Decryption: takes the same secret key that was used to encrypt and the ciphertext, returns the original plaintext
- Authentication and integrity
  - Authentication: guarantees the “identity” of the sender (e.g. MACs, signatures)
  - Integrity: guarantees that the received message is the same as the sent message (e.g. hash functions)

A cryptographic system is usually made up of many fundamental cryptographic algorithms called primitives.

# Kerchoff's principle

“The cryptographic key should be the only secret: it would be foolish to rely on our enemies not to discover what algorithms we use because they most likely will. Instead, let's be open about them.”

# Classification of encryption / decryption algorithms

## Symmetric cryptography

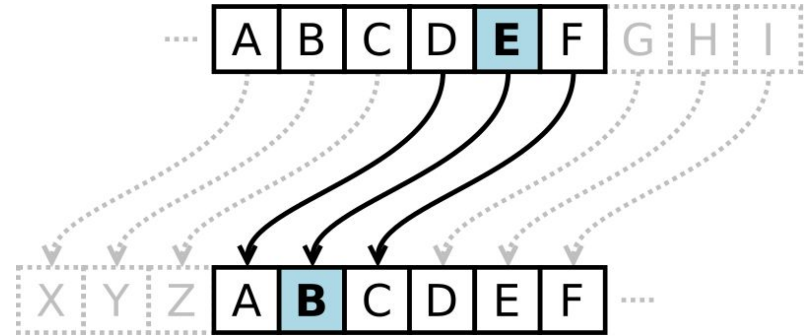
- The same key is used for encryption and decryption
- Basically making a lot of mess with bits
- Example: AES

## Asymmetric cryptography

- Different keys are used for encryption and decryption
- Based on difficult mathematical problems
- Example: RSA

# An easy example of encryption: Caesar cipher

- Encryption: shifting every letter in the message of  $x$  positions
- Decryption: shifting every letter in the message of  $x$  positions in the opposite direction
- Secret Key: the value of  $x$



plaintext  
“super secret message”

$x = -3$

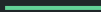
ciphertext  
“prmbo pbzobq jbppxdb”

**Challenge time**



# XOR

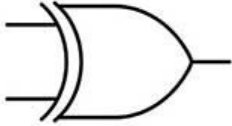
- Definition of the XOR operator
- The role of XOR in cryptography
- Why XOR?
- XOR Properties
- One time pad: how to encrypt with XOR



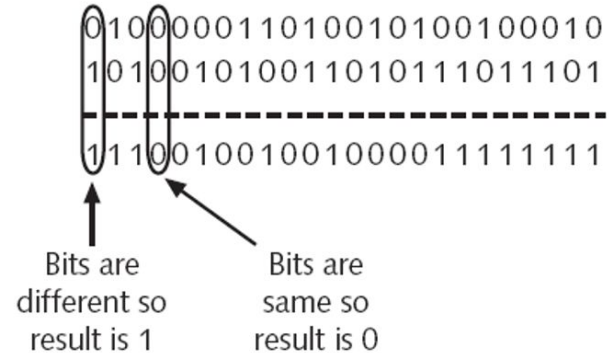
# Definition of the XOR operator

- XOR takes two inputs and returns an output
- It is a bitwise operation, which means each bit of the two inputs is processed separately, producing one bit of output, then the different outputs are concatenated, producing the final output

XOR



A	B	Output
0	0	0
1	0	1
0	1	1
1	1	0



# The role of XOR in cryptography

Some examples of cryptographic primitives which rely on the XOR operation:








- Hash functions (sha2, sha3...)
- Symmetric key encryption / decryption
  - Block ciphers (AES-CBC...)
  - Stream ciphers (AES-CTR, ChaCha20...)

...and many more!

# Why XOR?

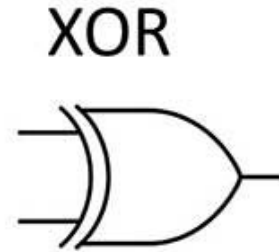
For a given plaintext bit (be it 0 or 1), the output is equally likely to be 0 or 1. So the ciphertext alone holds no information about the plaintext. This doesn't hold for other operators

Example: suppose we were using AND operator to encrypt a message, if a bit in the ciphertext is 1 we know for sure that the corresponding bit in the plaintext is 1 too.

Input		Output (Q)						
								
A	B	AND	OR	INH	XOR	NAND	NOR	XNOR
0	0	0	0	0	0	1	1	1
0	1	0	1	0	1	1	0	0
1	0	0	1	1	1	1	0	0
1	1	1	1	0	0	0	0	1

# XOR properties

- $a \oplus (b \oplus c) = (a \oplus b) \oplus c$
- $a \oplus b = b \oplus a$
- $a \oplus a = 0$
- $a \oplus 0 = a$
- $a \oplus b \oplus a = b$ 
  - $a \oplus b \oplus a =$
  - $a \oplus a \oplus b =$
  - $0 \oplus b =$
  - $b$



A	B	Output
0	0	0
1	0	1
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# One Time Pad: how to encrypt with XOR

We have a plaintext  $p$  and a key  $k$  the same size of the plaintext, we compute the ciphertext  $c$  as:

$$c = p \oplus k$$

Since  $a \oplus b \oplus a = b$ , the decryption works as follows:

$$c \oplus k = p \oplus k \oplus k = p$$

**Why do we need the key and the plaintext to be the same size?**

**Challenge time**

# Diffie-Hellman

- The problem of exchanging a shared secret key
- The Discrete Logarithm Problem
- DH Algorithm
- Attacks
  - Man in the Middle
  - Solving DLP





# The Problem

- Alice and Bob want to exchange messages over an insecure channel, while preventing others from reading them

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They have to find a way to share the secret key in a secure way

# The Solution

There are 2 main solutions to this problem:

- Use physical means or meet each other
- Use the same insecure channel with some math tricks:
  - Diffie-Hellman
  - RSA

# History

- The Diffie-Hellman key exchange is a cryptographic protocol that can securely generate a symmetric cryptographic key over a public channel
- It was published by Whitfield Diffie and Martin Hellman in 1976
- It was one of the first public key protocols



# Applications

- TLS/SSL
- SSH
- IPSEC
- VPN
- Bluetooth
- WPA3
- IoT Pairing
- Smart TV

# The Discrete Logarithm Problem

- Given three integers **g**, **c**, **p**, find an integer **x** that satisfies the following congruence:

$$g^x \equiv c \pmod{p}$$

- If **g** and **p** are chosen properly, this problem is considered to be unsolvable with modern computational power

# The Algorithm

- Alice and Bob agree on a prime number  $p$  and on a number  $g$  called generator modulo  $p$



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- Alice and Bob obtained a shared key to use

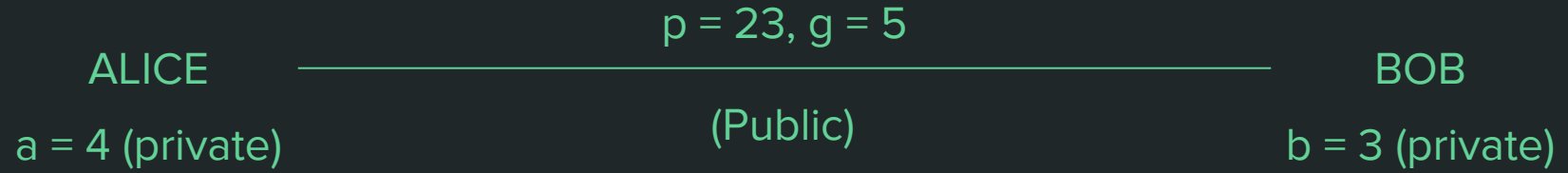
# **An easy example**

ALICE

$p = 23, g = 5$

(Public)

BOB






ALICE



$p = 23, g = 5$

$$A = 5^4 \pmod{23} = 4$$


BOB

ALICE   $p = 23, g = 5$  BOB

$A = 5^4 \pmod{23} = 4$

ALICE  BOB


$B = 5^3 \pmod{23} = 10$

ALICE   $p = 23, g = 5$  BOB  
 $A = 5^4 \pmod{23} = 4$

ALICE  BOB  
 $B = 5^3 \pmod{23} = 10$


ALICE   BOB

$$S_a = 10^4 \pmod{23} = 18$$



ALICE   $p = 23, g = 5$  BOB  
 $A = 5^4 \pmod{23} = 4$

ALICE  BOB  
 $B = 5^3 \pmod{23} = 10$

ALICE  BOB  
 $S_a = 10^4 \pmod{23} = 18$   $S_b = 4^3 \pmod{23} = 18$

ALICE   $p = 23, g = 5$  BOB  
 $A = 5^4 \pmod{23} = 4$

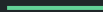
ALICE  BOB  
 $B = 5^3 \pmod{23} = 10$

ALICE  Shared key  BOB  
 $S_a = 10^4 \pmod{23} = 18$   $S_b = 4^3 \pmod{23} = 18$

**Challenge time**

# Attacks

- Man in the Middle
- Solving DLP



# Man in the Middle



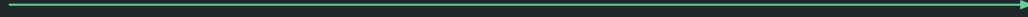
ALICE

$p, g$

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BOB

ALICE




BOB

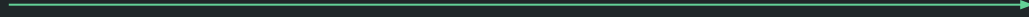


ALICE  → BOB

ALICE ←  BOB

ALICE  Shared key  → BOB

ALICE



BOB

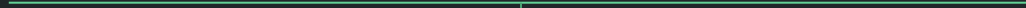
ALICE

BOB



CAROL

ALICE

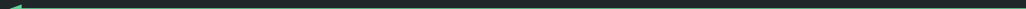


BOB



CAROL

ALICE



BOB



CAROL

ALICE

BOB



CAROL

ALICE

BOB



Shared key #1

CAROL



ALICE



BOB

CAROL

ALICE



BOB

CAROL

ALICE



BOB

CAROL

ALICE



BOB

CAROL

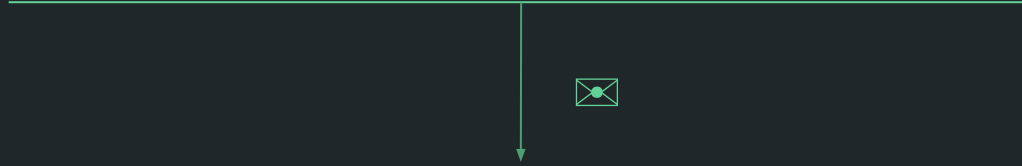
ALICE



BOB

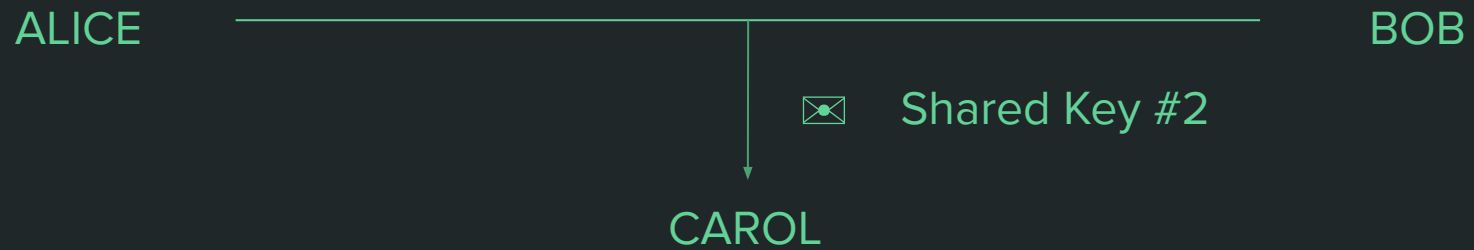
CAROL

ALICE

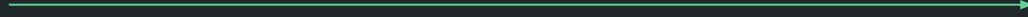


BOB

CAROL



ALICE



BOB

ALICE

BOB

Decrypt the  
message



CAROL

ALICE

BOB



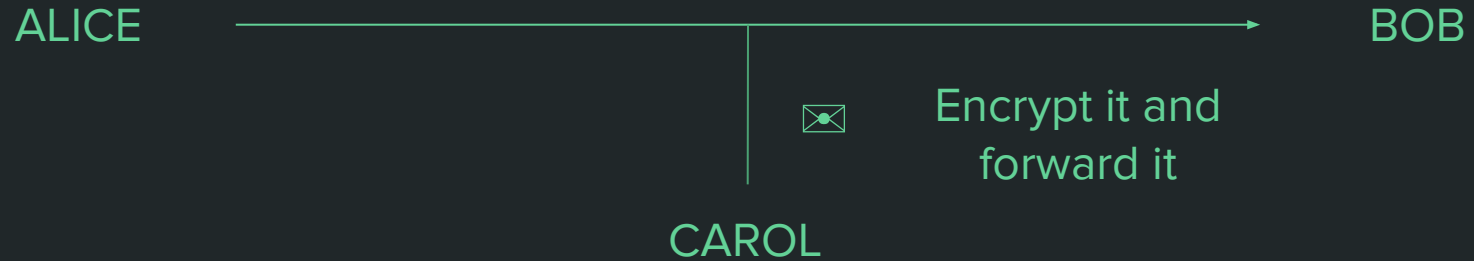
A diagram illustrating a communication channel. A horizontal line represents the channel between Alice and Bob. A vertical line with a downward-pointing arrow intersects this horizontal line, representing an eavesdropper, Carol.

CAROL



Read the plaintext





Carol using the keys generated with Alice and Bob, can easily eavesdrop over the channel

**Challenge time**

# Solving DLP

# Solving DLP

There are algorithms that try to solve the DLP:

- Baby step - Giant step
- Pohlig - Hellman
- Pollard's Rho
- Shor's algorithm